

AMS 7: Discussion Section 1

9/29 See handout for questions & additional info. Census.gov has population info.

1.(a)

year	# cancer deaths
1970	331,000 ←(old)
1985	462,000 ←(new)

1. absolute comparison → new - old
 ↳ unrelated to absolute value $462,000 - 331,000 = 131,000$ → there were 131K more cancer deaths in 1985 in the U.S. than 1970. (True)

2. Relative comparison → how much larger in percentage terms

$$\frac{\text{new} - \text{old}}{\text{old}} = \frac{131,000}{331,000} \doteq \frac{1}{3} = 0.33 = 33\%$$

by calculator: 0.3957703927
 ↳ 3 sig figs: 0.396 = +39.6% \doteq 40%

\doteq means "about equal to" There were 40% more cancer deaths in 1985 in the U.S. than in 1970.

Q: Can we say 40% fewer deaths?

let's try: $\frac{\text{old} - \text{new}}{\text{new}} = \frac{-131,000}{462,000} = -0.284 = 28.4\%$ Nope! There were 28% fewer cancer deaths in 1970 than in 1985 in the U.S.

• This cannot be attributed to population growth alone.

intuition: U.S. population rise in same period was smaller than 40%.



(b) variable: things you measure (your height is a variable of you)

cost/benefit tradeoff i.e. PSA is a cheap but inaccurate way to detect prostate cancer

circumference → radius → diameter (cheapest method)

height

volume $v = \pi r^2 h$ $v = \frac{1}{3} \pi r^2 h$

geometry models:   $I = m$

- (c)
- | | |
|---------|------------------------------|
| seattle | ⊗ cost of living (gas price) |
| omaha | ⊗ quality of mass transit |
| atlanta | ⊗ weather |
| | ⊗ crime rate |
| | ⊗ entertainment |

utility - how much you value something

(d) weight - yes height - no $\frac{\text{weight}}{\text{height}}$ - yes, but can have more errors

(e) $\frac{20 \text{ beats}}{15 \text{ sec}} \Bigg| \frac{60 \text{ sec}}{1 \text{ min}} = 80 \text{ b/m}$

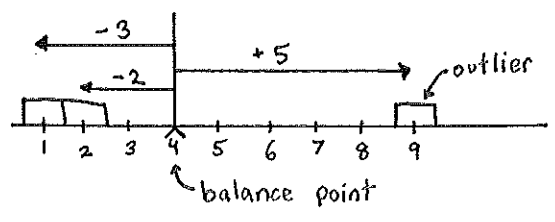
$$\frac{39 \text{ beats}}{30 \text{ sec}} \Bigg| \frac{60 \text{ sec}}{1 \text{ min}} = 78 \text{ b/m}$$

$$\frac{80 \text{ beats}}{65 \text{ sec}} \Bigg| \frac{60 \text{ sec}}{1 \text{ min}} = 73.85!$$

Section: 2c

$$\begin{bmatrix} 1 \\ 2 \\ 9 \end{bmatrix} n=3 \xrightarrow[\bar{y}=4]{\text{Subtract}} \begin{bmatrix} -3 \\ -2 \\ +5 \end{bmatrix} n=3$$

mean $\bar{y} = 4$ mean 0



$$\begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix} \xrightarrow[\bar{y}]{\text{subtract}} \begin{bmatrix} y_1 - \bar{y} \\ y_2 - \bar{y} \\ \vdots \\ y_n - \bar{y} \end{bmatrix}$$

old mean \bar{y} new mean 0?

$$\begin{aligned} \text{new mean: } \frac{(y_1 - \bar{y}) + (y_2 - \bar{y}) + \dots + (y_n - \bar{y})}{n} &= \frac{1}{n} \sum_{i=1}^n (y_i - \bar{y}) \\ &= \frac{1}{n} [(y_1 - \bar{y}) + (y_2 - \bar{y}) + \dots + (y_n - \bar{y})] \\ &= \frac{1}{n} \left[\underbrace{y_1 + y_2 + \dots + y_n}_{n\bar{y}} + \underbrace{(-\bar{y} - \bar{y} \dots - \bar{y})}_{-n\bar{y}} \right] = 0 \checkmark \end{aligned}$$

$$\text{mean } \bar{y} = \frac{1}{n} (y_1 + y_2 + \dots + y_n)$$

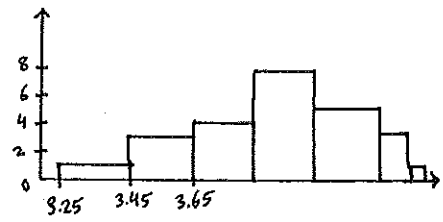
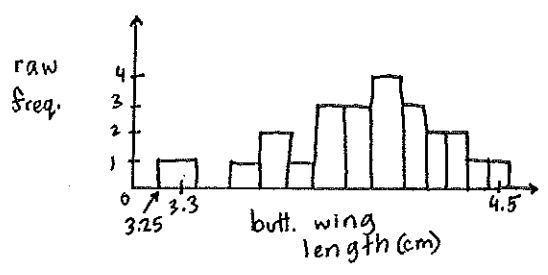
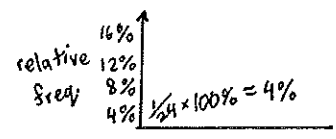
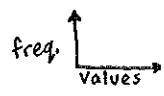
so $n\bar{y} = (y_1 + y_2 + \dots + y_n)$

Discussion Section # 2:

new grouping	value	(raw) freq. = count
1	3.3	1
	3.4	0
3	3.5	1
	3.6	2
4	3.7	1
	3.8	3
7	3.9	3
	4.0	4
5	4.1	3
	4.2	2
3	4.3	2
	4.4	1
1	4.5	1

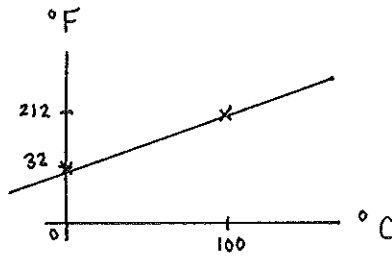
Sum = n = 24

Stem & leaf plot by Tukey



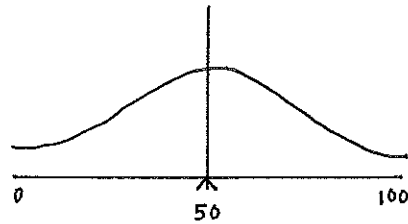
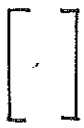
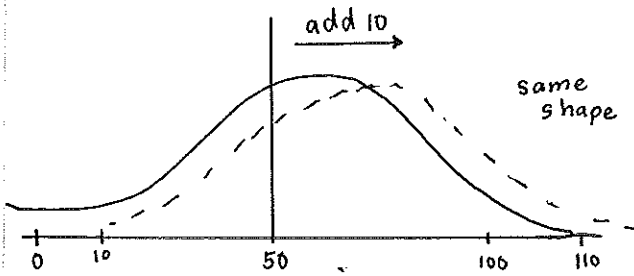
2.

°C	°F
0	32
100	212

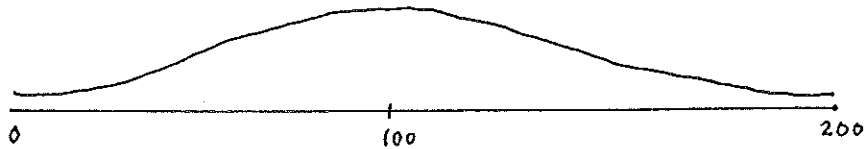


$$^{\circ}\text{F} = \frac{9}{5}^{\circ}\text{C} + 32$$

$$y = mx + b$$



multiply
by 2

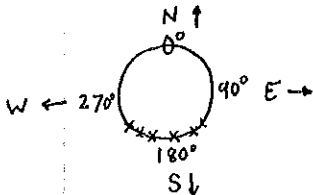


center changed - got
multiplied by 2

Spread got multiplied by 2

Same shape

compass degrees are...



- 170
- 205
- 187
- ⋮

quant.

continuous
no "twice as south"

interval scale